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Abstract

Active learning's key task is selecting informative data points to enhance model predictions with a fixed labeling budget. However, when ensemble models such as random forests are used, there is a risk of the ensemble containing models with poor predictive accuracy or redundant trees with the same interpretation. To address this, we develop a novel approach to only ensemble the set of nearoptimal models called the Rashomon set in order to guide the active learning process. We demonstrate how taking a Rashomon approach can not only improve the accuracy and rate of convergence of the active learning procedure, but also lead to improved interpretability compared to traditional approaches.

Contributions

Be careful what you average over

1. Incorporating implausible/poor trees

Most ensemble methods tend to aggregate over the space of all models, even if some of the models may have relatively poor accuracy.

2. Explanations \neq Trees



Methods/Algorithm

Algorithm 1: Unique Tree Farms Active Learning Input: $D_{trn}^{(0)}; D_{tst}; D_{cdd}^{(0)}; \epsilon;$ 1 repeat Train **F** on $D_{trn}^{(n)}$; Test **F** on $D_{tst}^{(n)}$; Enumerate \mathcal{R} with TreeFarms;

- (Optionally) Reduce the Rashomon set ${\cal R}$ to 5 the top k models in \mathcal{R} ;
- Predict labels $\hat{y}_{tst,m}^{(n)}$ from D_{tst} and calculate 6 the classification error for each tree f_m in \mathcal{R} :
- Define the smallest classification error 7 from amongst the trees in \mathcal{R} as the current iteration error;
- Compute vote-entropy $\delta^{(n)}(y, x, \mathcal{C})$ on $D_{cdd}^{(n)}$; 8

1. We enhance active learning by exclusively aggregating the most plausible decision trees of the Rashomon set, ensuring efficiency and relevance.

2. We improve interpretability by pruning redundant trees, providing a more comprehensive ensemble of distinct yet near-optimal models.

Active Learning

Labeling training data for machine learning models is expensive and time-consuming. Active learning (AL) reduces this burden by strategically selecting the most informative data points for labeling.



Figure 2. Multiplicity of explanations in decision trees.

Rashomon Decision Trees

The Rashomon set is a collection of models that are all near-optimal in predictive accuracy.

Definition 1 (Rashomon Set) Given a threshold ϵ , a hypothesis space \mathcal{F} , loss function \mathcal{L} , and reference model \hat{f} , a Rashomon set $\hat{\mathcal{R}}$ is defined as

> $\hat{\mathcal{R}} := \{ f \in \mathcal{F} : \mathcal{L}(f) \le (1 + \epsilon) \cdot \mathcal{L}(\hat{f}) \}$ (1)

Xin et al. were the first to introduce an algorithm (TreeFarms) that fully enumerates the Rashomon set for sparse decision trees [3].

Adaptation: To address Issue 2, we restrict our aggregation to trees with unique explanations in the Rashomon set:

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- Resample $B^{(n)}$ from $D_{cdd}^{(n)}$ based on the 9 observation with the highest vote entropy: $B^{(n)} := \arg \max_{x} \delta^{(n)}(y, x, \mathcal{C});$
- Query $B^{(n)}$ for oracle labeling; 10
- Update training and test set: 11

sufficiently small;

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3

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 $D_{trn}^{(n+1)} = D_{trn}^{(n)} \cup B^{(n)}; \ D_{cdd}^{(n+1)} = D_{cdd}^{(n)} \setminus B^{(n)}$ **12 until** labelling budget is depleted or test error is

Simulation Results



Results 1: Aggregeating over the Rashomon sets

Figure 1. Active learning diagram.

Informativity is measured by vote entropy:

$$\begin{split} \delta(y,\mathbf{x},\mathcal{C}) &= \max_{\mathbf{x}} - \sum_{y\in\mathcal{Y}} \frac{\text{vote}_{\mathcal{C}}(y,\mathbf{x})}{|\mathcal{C}|} \log \frac{\text{vote}_{\mathcal{C}}(y,\mathbf{x})}{|\mathcal{C}|} \\ \text{where} \end{split}$$

$$\mathsf{vote}_{\mathcal{C}}(y, \mathbf{x}) = \sum_{c \in \mathcal{C}} \mathbb{I}\{c(\mathbf{x}) = y\}$$

is the number of "votes" that label y receives for covariate \mathbf{x} from the members c of committee \mathcal{C} .

The base learners in ensemble methods naturally form a committee, with disagreement in "votes" serving as a common uncertainty metric. However, redundant trees with duplicate explanations can artificially inflate agreement in the committee [1].



Figure 3. A depiction of how to ensemble Rashomon trees.

outperform random forest by a significant margin.

Result 2: Pruning to only retain trees with unique explanations improves interpretability while maintaining predictive accuracy.

Future Work

Unlike TreeFarms, Rashomon Partition Sets [2] exhaustively enumerate the Rashomon set without relying on a predefined geometry, offering potential for active learning applications.

References

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https://thmccormick.github.io/

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